

Chapter 7 § 2

The Pythagorean Theorem and Its Converse

Definitions :

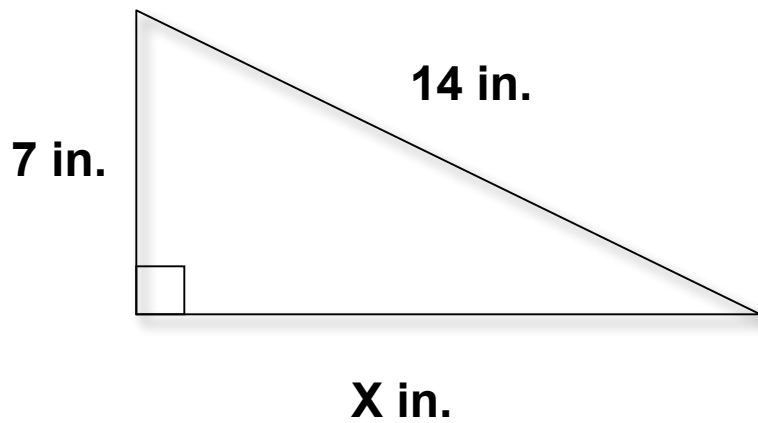
Pythagorean Triple – a group of three whole numbers that satisfies the equation $a^2 + b^2 = c^2$, where c is the greatest number.

Theorems :

Pythagorean Theorem (7-4) – In a right triangle, the sum of the squares of the measures of the legs equals the square of the measure of the hypotenuse.

Converse of the Pythagorean Theorem (7-5) – If the sum of the squares of the measures of two sides of a triangle equals the square of the measure of the longest side , then the triangle is a right triangle.

Find x



$$7^2 + x^2 = 14^2$$

$$49 + x^2 = 196$$

$$x^2 = 147$$

$$x \approx 12.12$$

Given $\triangle DAR$ with vertices $D(-3,6)$, $A(5, 5)$, and $R(3,2)$ determine if the triangle is a right triangle.

$$D = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

\overline{DA}

$$\sqrt{(5 - -3)^2 + (5 - 6)^2}$$

$$\sqrt{65}$$

\overline{DR}

$$\sqrt{(-3 - 3)^2 + (6 - 2)^2}$$

$$\sqrt{52}$$

\overline{AR}

$$\sqrt{(5 - 3)^2 + (5 - 2)^2}$$

$$\sqrt{13}$$

$$(\sqrt{13})^2 + (\sqrt{52})^2 = (\sqrt{65})^2$$

$$13 + 52 = 65$$

$$65 = 65$$

Therefore $\triangle DAR$ is a right triangle

Determine whether each set of numbers can be the measures of the sides of a right triangle. Then determine whether they form a Pythagorean triple.

9, 40, 41

$$9^2 + 40^2 = 41^2$$

$$81 + 1600 = 1681$$

$$1681 = 1681$$

yes, yes

$$\frac{9}{5} \quad \frac{12}{5} \quad 3$$

$$\left(\frac{9}{5}\right)^2 + \left(\frac{12}{5}\right)^2 = 3^2$$

$$\left(\frac{81}{25}\right) + \left(\frac{144}{25}\right) = 9$$

$$9 = 9$$

yes, no